

**Finding the vertex of a parabola in standard form**

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$$\hat{=} 2a = \frac{-110}{2(4)}$$

$$(-2, ) = -\frac{16}{8} = -2$$

$$y = 4(-2)^2 + 16(-2) + 20$$

$$4(4) + (-32) + 20$$

$$= 16 + 20 - 32$$

$$=$$

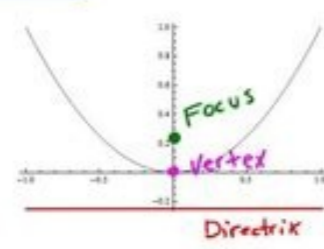
Find Vertex, Focus, Directrix of a Parabola

Parabola is:  $2x^2 - 16x + 35$

Vertex is the point:  $(h, k) = ?$

Focus is the point:  $(h, k + \frac{1}{4a})$

Directrix is the line:  $y = k - \frac{1}{4a}$



$$2x^2 - 16x + 35 \text{ write as } 2(x + (h)) + (k)$$

$$2(x^2 - 8x) + 35$$

$$2(x^2 - 8x + (\frac{8}{2})^2) + 35 - 2(\frac{8}{2})$$

## Graphing Parabolas in Standard Form

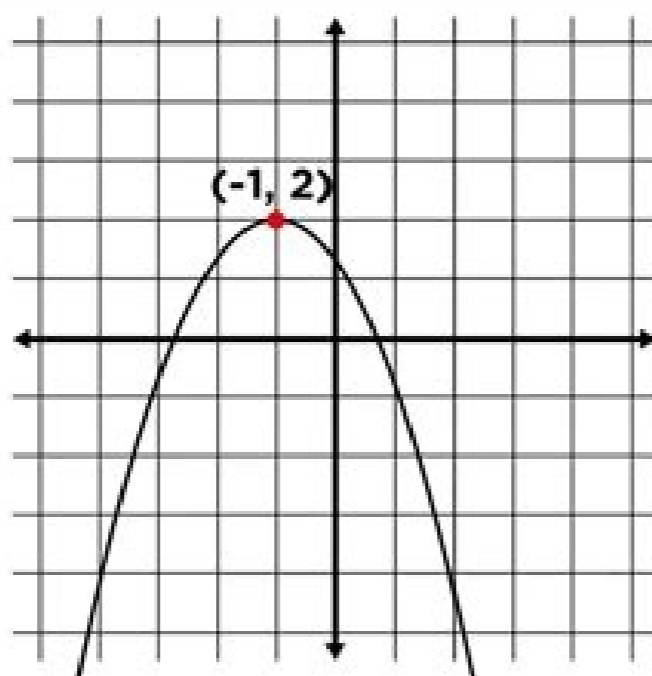
$$f(x) = -x^2 - 2x + 1$$

$$f(x) = -(x^2 + 2x) + 1$$

$$f(x) = -(x^2 + 2x + 1) + 2$$

$$f(x) = -(x + 1)^2 + 2$$

we can also complete the square manually



For the following quadratic equations, identify  $a$ ,  $b$  and  $c$ , and then find the equation for the line of symmetry.

Sample #1:  $y = x^2 + 6x - 5$

Sample #2:  $y = -2x^2 - 5x + 7$

Answer:  $a = 1, b = 6, c = -5$

Answer:  $a = -2, b = -5, c = 7$

The line of symmetry:

$$x = \frac{-b}{2a}$$

$$x = -3$$

The line of symmetry:

$$x = \frac{-(-5)}{2(-2)}$$

$$x = -\frac{5}{4}$$

1.  $y = x^2 + 4x + 12$

2.  $y = x^2 + 10x - 3$

3.  $y = x^2 - 12x + 4$

4.  $y = 2x^2 + 8x - 5$

5.  $y = -3x^2 + 6x - 1$

6.  $y = -x^2 - 2x - 2$

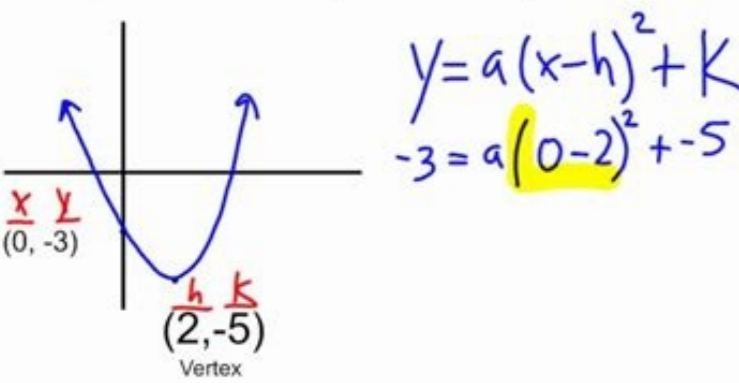
7.  $y = x^2 + 3x - 8$

8.  $y = 4x^2 - 16$

9.  $y = -8x^2$

10.  $y = 2x^2 - 7x$

Example 2 Write the equation of the parabola in vertex form.



How do you find the vertex of a parabola in standard form. Finding the vertex of a parabola in standard form calculator. Finding the vertex of a parabola in standard form worksheet. How to find the standard form of a parabola given the vertex and focus. Finding the vertex of a parabola in standard form khan academy. How to find the vertex in a standard form.

Save article as Article A series of points on a flat surface forming a curve such that each point on the curve is equidistant from the focus is a parabola is a straight line used to create the curve. The standard form of the parabolic equation is  $y = ax^2 + bx + c$ . Given the values of  $a$ ,  $b$  and  $c$ ; Our task is to find the coordinates of the vertex, the focus and the equation of the leading line. 198 See formula below for explanation. To continue using our website, we ask you to confirm your identity as a human being. Thank you for your cooperation. To continue using our website, we ask you to confirm your identity as a human being. Thank you for your cooperation. The vertex of a parabola is the highest or lowest point, also called the maximum or minimum of the parabola. is the maximum or minimum value of the parabola (see the figure below) This depends on whether the equation is at a vertex or in standard form x-coordinates of the vertices can be given as  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  can be found, and to get the y value of the vertex, just substitute  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  into the equation. In this mini-lesson we will look at the process of converting the standard form to the vertex form and vice versa. The standard parabola shape is  $y = ax^2 + bx + c$ , and the parabola vertex shape is  $y = a(x - h)^2 + k$ . Here the vertex shape includes a square. So to convert the standard to a vertex shape, we need to complete the square. Let's learn more about converting standard form to vertex form along with other examples. Standard and vertex forms of a parabola

Equation of a parabola Improve article Save article A series of points on a flat surface forming a curve such that every point on the curve is equidistant from the focus is a parabola. The vertex of the parabola is the coordinate from which it creates the tightest curve, while it is the straight line used to create the curve. The standard form of the equation of a parabola. Given the values of  $a$ ,  $b$  and  $c$ ; Our task is to find the coordinates of the vertex, focus and guide equation. Example - Input: 5 3 2 Output: Top: (4.3, 1.55) Focus: (4.3, 1.6) Guide:  $y = 198$  See formula below for explanation. In order to continue using our site, we ask you to verify your identity as a person. Thank you for cooperating. In order to continue using our site, we ask you to verify your identity as a person. Thank you for cooperating. The vertex of a parabola is the highest or lowest point, also known as the maximum or minimum of the parabola. - the maximum or minimum value of the parabola (see the figure below) - the inflection point of the parabola the axis of symmetry intersects the vertex (see the figure below) It depends on whether the equation has a vertex or the standard shape of the vertex can be given by the formula  $x = \frac{-b}{2a}$  can be found and to get the y-value of the vertex just type  $\frac{-b}{2a}$  into the field. Not for nothing is it called the "breakup shape"! The tip is just (h, k) from Eq. RadfordMathematics.com online math book In this mini-tutorial, we'll look at the process of converting standard form to vertex form and vice versa. The standard shape of a parabola Equation of a parabola can be represented in several ways such as: standard shape, top shape, and capture shape. One of these forms can always be converted to the other two forms depending on the requirements. In this article, we will learn how to convert a standard shape to a vertex shape and a vertex shape to a standard shape. First, let's see what each of these forms means. Standard form The standard form of a parabola is: Here  $a$ ,  $b$  and  $c$  are real numbers (constant), where  $a \neq 0$ .  $x$  and  $y$  are variables, where  $(x, y)$  represents a point on the parabola. Vertex shape The shape of the parabola's vertex is as follows: Here  $a$ ,  $h$  and  $k$  are real numbers, where  $a \neq 0$ .  $x$  and  $y$  are variables, where  $(x, y)$  represents a point on the parabola. How to convert a standard shape to a vertex shape? The vertex form  $y = a(x - h)^2 + k$  is a "whole square". So to convert the standard shape to the vertex shape, we just need to complete the square. But in addition, we also have a formula method to do this. Let's look at both methods. Completing the square Let's take as an example a parabola in standard form:  $y = -3x^2 - 6x - 9$  and convert it to the shape of a vertex, completing the square. First, we need to make sure that the x2 multiplier is 1. If the x2 multiplier is NOT 1, we put the number on the outside as a common factor. We get:  $y = -3x^2 - 6x - 9 = -3(x^2 + 2x + 3)$  Now the x2 factor is 1. Here are the steps to convert the above expression into vertex form. Step 1: Determine the x factor. Step 2: Divide it in half and square the resulting number. Step 3: Add and subtract the above number after the word x in the expression. Step 4: Factor the perfect square trinomial formed by the first three terms using the appropriate identity. Here we can use  $x^2 + 2xy + y^2 = (x + y)^2$ . In this case,  $x^2 + 2x + 1 = (x + 1)^2$  The above expression from step 3 becomes: Step 5: Simplify the last two numbers and divide the outer number. Here  $-1 + 3 = 2$ . So the above expression reads: This is the form  $y = a(x - h)^2 + k$ , which has a vertex form. Here the vertex is  $(h, k) = (-1, 2)$ . Using the formula in the method above, we could end up finding the values of  $h$  and  $k$  that help convert the standard shape to a vertex shape. But the values of  $h$  and  $k$  can easily be found using the following steps: Find  $h$  using  $h = -b/2a$ . Since  $(h, k)$  lies on the given parabola,  $k = ah^2 + bh + c$ . Just use that to find  $h$  to plug in the "h" value from the above step. Let's convert the same example  $y = -3x^2 - 6x - 9$  to standard form using this formula. Comparing this equation with  $y = ax^2 + bx + c$  gives  $a = -3$ ,  $b = -6$  and  $c = -9$ . Then (i)  $h = -b/2a = -(-6)/(2 \cdot -3) = -1$  (ii)  $k = -3(-1)^2 - 6(-1) - 9 = -3 + 6 - 9 = -6$  Substituting these two values (along with  $a = -3$ ) as the vertex  $y = a(x - h)^2 + k$  gives  $y = -3(x + 1)^2 - 6$ . Note that we get the same answer as a second method. Which way is easier? Decide and act. Tips and Tricks: If the above processes seem complicated, do the following: Compare this equation to the standard form ( $y = ax^2 + bx + c$ ) and get the values of  $a$ ,  $b$ , and  $c$ . Use the following formulas to find the values of  $h$  and  $k$  and substitute them as the vertex ( $y = a(x - h)^2 + k$ ):  $h = -b/2a$   $k = -D/4a$  Here  $D$  is the discriminant where  $D = b^2 - 4ac$ . How to convert vertex shape to standard shape? To convert the vertex shape to standard form, we just algebraically simplify  $a(x - h)^2 + k$  to get  $ax^2 + bx + c$ . Technically, we need to do the following steps to convert the vertex shape to standard form. Expand the square. (x-h)2. Agreement "and". Match similar words. Example: Convert the equation  $y = -3(x + 1)^2 - 6$  from vertex to standard form by following the steps above:  $y = -3(x + 1)^2 - 6 = -3(x + 1)(x + 1) - 6 = -3(x^2 + 2x + 1) - 6 = -3x^2 - 6x - 3 - 6 = -3x^2 - 6x - 9$  Important notes about standard vertex form: In vertex form,  $(h, k)$  represents the vertex of the parabola where the parabola has its maximum/minimum value. If  $a > 0$ , the minimum value of the parabola is  $(h, k)$ , and if  $a < 0$ , the maximum value of the parabola is  $(h, k)$ . Related Topics: Vertex Calculator Quadratic Calculator Example 1. Find the vertex of the parabola  $y = 2x^2 + 7x + 6$  by filling in the square. Solution: The given parabola equation is  $y = 2x^2 + 7x + 6$ . To find its vertex, we transform it into a vertex form. To complete the square, we first set the x2 multiplier to 1. We take the x2 multiplier (which in this case is 2) as the common multiplier.  $2x^2 + 7x + 6 = 2(x^2 + 7/2x + 3)$  x-factor is 7/2, half is 7/4, and its square is 49/16. By adding and subtracting it from the square polynomial in parentheses in the previous step,  $2x^2 + 7x + 6 = 2(x^2 + 7/2x + 49/16 - 49/16 + 3)$  Factorization of the square polynomial  $x^2 + 7/2x + 49/16$ , we get  $(x + 7/4)^2$ . Then  $2x^2 + 7x + 6 = 2((x + 7/4)^2 - 49/16 + 3) = 2((x + 7/4)^2 - 1/16) = 2(x + 7/4)^2 - 1/8$  Comparing this with  $(x - h)^2 + k$ , we get  $(h, k) = (-7/4, -1/8)$ . Answer: The vertex of this parabola is  $(-7/4, -1/8)$ . Example 2: Find the vertex of the same parabola as in example 1 without modifying the shape of the vertex. Solution: Given a parabola  $y = 2x^2 + 7x + 6$ . So  $a = 2$ ,  $b = 7$  and  $c = 6$ . The x-coordinate of the vertex is  $h = -b/2a = -7/(2 \cdot 2) = -7/4$ . The y-coordinate of the vertex is  $k = 2(-7/4)^2 + 7(-7/4) + 6 = -1/8$ . Answer: We have the same answer as in example 1, namely  $(h, k) = (-7/4, -1/8)$ . Example 3: Find the equation of the following parabola in standard form. Solution: We see that the parabola has its greatest value at  $(2, 2)$ . So, the vertex of the parabola is  $(h, k) = (2, 2)$ . Thus, the shape of the vertex of the above parabola is  $y = a(x - 2)^2 + 2$ . (1). To find "a" here, you need to substitute any known point on the parabola into this equation. The schedule is clear(1, 0) = (x, y). Substitute it into (1):  $0 = a(1 - 2)^2 + 2 \cdot 0 = a + 2$   $a = -2$ . Substitute back into (1) and expand the square to bring it to standard form:  $y = -2(x - 2)^2 + 2 = -2(x^2 - 4x + 4) + 2 = -2x^2 + 8x - 8 + 2 = -2x^2 + 8x - 6$  Answer: The standard form of this parabola is:  $y = -2x^2 + 8x - 6$ . View Answer > Skip to Slide Skip to Slide Great Middle School Teaching with Simple Tips When you're cramming, you're more likely to forget concepts. With Cuemath you will learn visually and be amazed by the results. Book a Free Trial Lesson Standard Shape to Vertex Shape Frequently Asked Questions To convert a standard shape to vertex shape, convert  $y = ax^2 + bx + c$  to  $y = a(x - h)^2 + k$  to fill in the square. Then  $y = a(x - h)^2 + k$  is a vertex form. How to convert vertex shape to standard shape? Converting a vertex shape to a standard shape is very easy. Just expand the square at  $y = a(x - h)^2 + k$ , then expand the brackets, and finally simplify. How to convert standard form to vertex form using quadratic completion? To convert a standard shape to a vertex shape using the square fill method, take the x2 factor as the common factor if it is different from 1. Divide the x factor in half and square it. Add and subtract this number from the square of the first step. Then apply algebraic identities and write them down as vertices. How to find the vertex of a parabola in standard form? The vertex cannot be directly identified from the standard form. Convert the standard form to the vertex form  $y = a(x - h)^2 + k$ , then  $(h, k)$  gives the vertex of the parabola. How to convert a standard shape to a vertex shape without completing a square? To convert  $y = ax^2 + bx + c$  to  $y = a(x - h)^2 + k$  without completing the square, just find "h" and "k" using the following formulas:  $h = -b/2a$   $k = -(b^2 - 4ac)/4a$  What is the use of converting a standard shape to a vertex one? The vertex form is more useful when plotting quadratic functions where we can do it easily, vertex, and by finding one or two points on each side of the vertex, the ideal shape of the parabola could be obtained. Parabola.



